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This manuscript provides a step-by-step guide to statistical power calculation for the fixed effects of analysis of variance (ANOVA) designs with an equal number of observations in each cell. A brief history of ANOVA hypothesis testing theory is included to explain why power calculation is important and how the results can be used. The relationship between lambda (λ), the noncentrality parameter used to calculate power in the ANOVA, and Cohen's (1988) measure of effect size is provided. Algorithms are provided for power calculation and for conversion between λ , Cohen's measure of effect size, and <u>phi</u>—the parameter used in many tables of the noncentral <u>F</u> The appendices contain power of calculation examples for the main and interaction effects of 2 x 3 x 3 between- and within- subjects designs.

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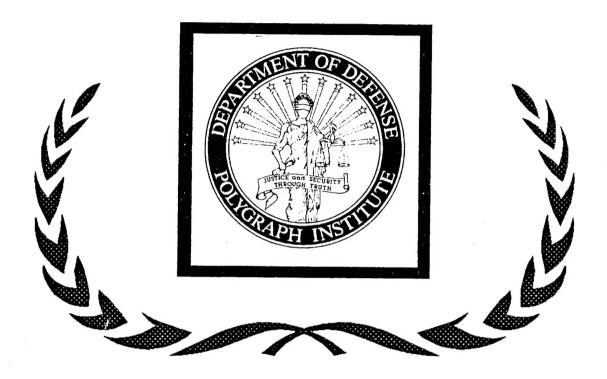
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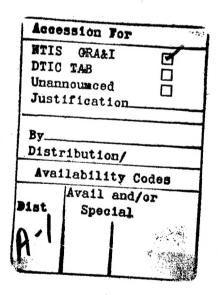
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A Computational Guide to Power Analysis of Fixed Effects in Balanced Analysis of Variance Designs

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September 1995



Director's Foreword

The results of numerous published studies, both within and outside of the psychophysiological detection of deception (PDD) literature, are based on observation groups which are too small to provide results that are representative of the general population. Such studies are described as having low or insufficient statistical power. These publications not only represent a misuse of potentially useful resources, but may lead to unjustified, if not erroneous, conclusions. Among the potential reasons for the prevalence of such studies in the literature are the limited awareness of statistical power analysis, and difficulty associated with the calculation of statistical power.

This manuscript is the first of several computational guides to statistical power analysis to be developed at the Institute. It is designed to assist the investigator in designing, and understanding the analysis of, fixed effects in balanced factorial analysis of variance statistical designs. Future guides will address statistical power calculation for the commonly used student— \underline{t} and chi-square inferential statistics. This and future documents should assist others, as they have the DoDPI faculty, in both the design and evaluation of PDD investigations.

John R. Schwartz Acting Director

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Abstract

DOLLINS, A. B. A computational quide to power analysis of fixed effects in balanced analysis of variance designs, September 1995, Report No. DoDPI95-R-0003. Department of Defense Polygraph Institute, Ft. McClellan, AL 36205. -- This manuscript provides a step-by-step guide to statistical power calculation for the fixed effects of analysis of variance (ANOVA) designs with an equal number of observations in each cell. A brief history of ANOVA hypothesis testing theory is included to explain why power calculation is important and how the results can be used. The relationship between lambda (λ) , the noncentrality parameter used to calculate power in the ANOVA, and Cohen's (1988) measure of effect size is provided. Algorithms are provided for power calculation and for conversion between λ , Cohen's measure of effect size, and phi--the parameter used in many tables of the noncentral F distribution. The appendices contain power calculation examples for the main and interaction effects of 2 x 3 x 3 between- and withinsubjects designs.

Key Words: Computation guide, analysis of variance (ANOVA), statistical power, lambda (λ) , alpha (α) , beta (β) , effect size, algorithm.

Executive Summary

DOLLINS, A. B. <u>A computational guide to power analysis of fixed effects in balanced analysis of variance designs</u>, September 1995, Report No. DoDPI95-R-0003. Department of Defense Polygraph Institute, Ft. McClellan, AL 36205.

The power of a statistical test is the probability that the test will correctly reject the null hypothesis. Statistical power is commonly used to calculate the number of observations necessary to yield statistically significant results or to calculate the probability that a statistically significant effect would have been found if one existed. The power of a statistical test should not be confused with the significance of a statistical test--which is the probability that a true null hypothesis is falsely rejected. It is possible to obtain statistically significant effects with low or high power. text books concerning statistics describe power calculation procedures, but they are usually brief, sometimes difficult to understand, and occasionally misleading. This manuscript is an attempt to provide a clear, easy to understand, step-by-step guide to the calculation of statistical power for fixed effects of analysis of variance (ANOVA) designs with an equal number of observations in each cell. A brief history of ANOVA hypothesis testing theory is presented to explain why power calculation is important and how its results can be used. The confusing issue of whether a hypothesis may only be rejected, versus rejected or accepted, is explained. The relationship between lambda (λ) , the noncentrality parameter used to calculate power in the ANOVA, and Cohen's (1988) measure of effect size is provided. Algorithms are provided for power calculation and for conversion between λ , Cohen's measure of effect size, and phi--the parameter used in many tables of the noncentral \underline{F} distribution. The appendices contain power calculation examples for the main and interaction effects of 2 x 3 x 3 between- and withinsubjects designs.

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Scheffe (1959, p. 3) roughly defines the analysis of variance (ANOVA) as "a statistical technique for analyzing measurements depending on several kinds of effects operating simultaneously, to decide which kinds of effects are important and to estimate the effects." Scheffe (1959, p. 3) attributes the development of ANOVA techniques chiefly to R. A. Fisher (1918, 1935), who was attempting to address agricultural rather than psychological research.

In practice, the ANOVA is a set of procedures for calculating the probability that a particular set of observations could have occurred by chance (i.e., randomly). Thus, a hypothesis may be rejected, with some degree of confidence, that a similar set of observations would not occur by chance. The hypothesis tested is usually the null hypothesis that two or more means (dependent variables), observed during two or more experimental manipulations (independent variables) are equal. This hypothesis may only be rejected (i.e., the groups of values are not equal) based on the ANOVA of the observed values. It is important to note that failure to reject a hypothesis does not, according to Fisherian logic, indicate acceptance of the hypothesis (Fisher, 1966, p. 16). (Cohen [1990] argues that this is a flaw in Fisherian logic because the null hypothesis is always false in the real world - given a large enough sample size.) If the probability that the observed values could have occurred by chance is less than a preset probability level (i.e., referred to as the significance criterion or alpha $[\alpha]$), the null hypothesis is rejected.

Neyman and Pearson (1928a, 1928b) proposed that the specification of an alternative hypothesis be added to the (This concept was, according to Cohen [1990, p. 1307], violently opposed by Fisher.) Inclusion of an alternative hypothesis, to be accepted if the null hypothesis was rejected, revolutionized the decision process associated with the ANOVA. Now the ANOVA could be used to both support and reject hypotheses. Including an alternative hypothesis, with an associated effect size, allows the calculation of the probability that the null hypothesis is not rejected when it is false, as well as the probability of rejecting the null hypothesis, given that the alternative hypothesis is true-referred to as beta (β) or Type II error. Calculation of β allows calculation of its compliment (i.e., $1 - \beta$), power, the probability that the null hypothesis is correctly rejected. probability that the null hypothesis will be rejected when it is true, alpha (α) , is referred to as the Type I error rate.

The number of observations necessary to support a hypothesis can thus be calculated--given the desired α and β probabilities and the magnitude of the difference between the null and alternate hypotheses. The power of an ANOVA test can also be calculated--given the desired α level, the number of

observations, and the magnitude of the difference between the null and alternate hypotheses. Power analysis is primarily used to determine the probability that a statistically significant difference will be obtained, given a specified difference among the observations, and a specified number of observations; or the probability that a statistically significant effect would have been obtained (where none is found) if one had existed. it is possible to calculate and use the parameters necessary to support a hypothesis with a relatively high degree of confidence it is, apparently, rarely done. This is documented by the relatively low power (< .60) of the majority of studies, in numerous research fields, to detect small and medium effects (Bones, 1972; Brewer 1972; Brewer & Owne, 1972; Brown & Hale, 1992; Chase & Tucker, 1975; Chase & Chase, 1976; Chase & Barnum, 1976; Christensen & Christensen, 1977; Cohen, 1962; Crane, 1976; Daly & Hexamer, 1983; Fagley, 1985; Frieman, Chalmers, Smith, & Kuebler, 1978; Haase, 1974; Haase, Waechter, Solomon, 1982; Hall, 1982; Jones & Brewer, 1972; Julnes & Mohr, 1989; Kosciulek, 1993; Kosciulek & Szymanski, 1993; Kroll & Chase, 1975; Orme & Combs-Orme, 1986; Orme & Tolman, 1986; Ottenbacher, 1982; Penick & Brewer, 1972; Rossi, 1990; Rothpearl, Mohs, & Davis, 1981; Sawyer & Ball, 1981; Sedlmeier & Gigerenzer, 1989; Wolley, 1983; Wooley & Dawson, 1983). According to S. E. Edgell (personal communication, August 14, 1995) the main problem with low power is that the researcher wastes time by running studies that have little chance of finding the result desired.

Perhaps one of the reasons that the power of \underline{F} ratios are. not calculated or reported more frequently is the difficulty associated with power calculations. Calculating the power of F ratios in ANOVA designs can be difficult, particularly for designs with more than one factor and/or repeated factors, because the majority of the calculations must be completed by The most complete text on the topic of power analysis is Jacob Cohen's Statistical Power Analysis for the Behavioral Sciences (1988) -- which addresses power calculation for most commonly used parametric and non-parametric statistics. Unfortunately, Cohen's (1988) calculations for the ANOVA (pp. 273-406, 550-551) are appropriate for one-way ANOVA designs but underestimate the power and overestimate the sample sizes of higher level designs (Koele, 1982). (Note: Koele was referring to the calculations described in the 1977 edition of Cohen's book - which remain the same in the more current 1988 version.) As can be seen in Appendices B and C, this is true for betweensubjects designs, but the reverse is true for within-subjects Cohen (1988) does not describe power calculations for repeated measure ANOVA designs in any detail, but suggestions may be found elsewhere (Bavry, 1991, pp. 63-76; Davidson, 1972, p. 448; Koele, 1982; Kraemer & Thiemann, 1987, pp. 45-52; Lipsey, 1990, pp. 79-84; Winer, 1971, p. 516).

Cohen (1988) does, however, note several important observations concerning power analysis. Statistical significance levels have generally been set by convention to .05 or .01 (Cowles & Davis, 1982). No such convention exists for power levels, however, Cohen (1988, p. 56) suggests that the value of .80 be used when the investigator has no other basis for setting the desired power value. Cohen (1988, pp. 284-288, 355) further proposes that ANOVA effect sizes, for the behavioral sciences, be categorized into small (.10), medium (.25), and large (.40) for theoretical purposes. Cohen (1988, pp. 364-367) also notes that it is possible to calculate power for separate effects of a complex factorial design independently. This is somewhat analogous to the independent calculation of the effects in a complex factorial design.

The following quide to calculating the power of fixed effects in balanced ANOVA design F tests is designed to summarize what can be a very confusing process. The works of Bavry (1991), Borenstein and Cohen (1988), Cohen (1988), Koele (1982), and Winer (1971) were relied upon most heavily during the development of this quide. It should be noted that the processes described herein are based primarily on statistical theory rather than empirical evidence. Monte Carlo studies of the statistical power of ANOVA designs have, however, been reported (Cole, Maxwell, Arvey, & Salas, 1994; Cornell, Young, Seaman, & Kirk, 1992; Keselman, Rogan, Mendoze, & Breen, 1980; Klockars & Hancock, 1992). The description below pertains only to power analysis of a complex fixed effect between- and withinsubjects factorial ANOVA designs with an equal number of observations in each cell (Cohen's, 1988, case 2). Adjustments for an unequal number of observations in each cell are described by Cohen.

Power Calculation

To calculate the power of the \underline{F} ratio of a complex fixed effect ANOVA design, it is necessary to know the: significance criterion of the \underline{F} ratio for which power is calculated (α); degrees of freedom of the numerator of the \underline{F} ratio for which power is calculated; degrees of freedom of the denominator of the \underline{F} ratio for which power is calculated; and, the noncentrality parameter associated with the \underline{F} ratio. As detailed below, the noncentrality parameter can be calculated using Cohen's effect size- $\underline{-f}$ (1988). If predicting the power of a repeated measure design using data from a between-subjects design, it is also necessary to calculate the (assumed constant) correlation between pairs of observations on the same element and factor level, as detailed below.

According to Koele (1982), the power of a fixed effect ANOVA \underline{F} test is the probability that ($\underline{F} > \underline{F}\underline{C}$ given $\underline{d}\underline{f}\underline{1}$, lambda $[\lambda]$). Koele defines λ as the noncentrality parameter;

 $\underline{df1}$ and $\underline{df2}$ as the numerator and denominator, respectively, degrees of freedom of the \underline{F} ratio for which power is being calculated, and \underline{Fc} as the critical \underline{F} value (with $\underline{df1}$ and $\underline{df2}$ degrees of freedom) that the \underline{F} ratio must exceed at a given significance level. It is distributed as a noncentral \underline{F} distribution.

Significance Criterion / Fc - Critical F Value

 \underline{Fc} is the \underline{F} ratio, associated with a given probability (α) level which the calculated \underline{F} statistic must exceed to be significantly different from chance. For instance, an observed \underline{F} ratio with $\underline{df1}=3$ and $\underline{df2}=20$ must exceed $\underline{Fc}=3.10$ to be statistically significant at an α level of 0.05 and must exceed $\underline{Fc}=4.94$ to be statistically significant at an α level of 0.01. This value can be calculated from the central \underline{F} distribution given the α level and the numerator and denominator degrees of freedom. It can also be obtained from tables of the central \underline{F} distribution given in most textbooks of statistical analyses (e.g. Winer, 1971; Keppel, 1991).

Numerator Degrees of Freedom - df1

These are the degrees of freedom associated with the numerator of the \underline{F} ratio for which power is calculated.

<u>Denominator Degrees of Freedom - df2</u>

These are the degrees of freedom associated with the denominator of the \underline{F} ratio for which power is calculated.

The Noncentrality Parameter - λ

The noncentrality parameter is equal to the \underline{F} statistic numerator sum of squares, with each term replaced by its expectation, divided by the within-cells error variance (i.e., the mean squares error term; Kendall & Stuart, 1966, p. 5; Scheffe, 1959, p. 39). The noncentrality parameter, λ is thus equal to the calculated \underline{F} ratio times its numerator degrees of freedom. For example, the λ associated with $\underline{F}(2, 8) = 63.389$ would be 2 * 63.389 or 126.778, and the λ associated with $\underline{F}(4, 16) = 0.357$ would be 4 * 0.357 or 1.427 (see Appendices A, B, and C for more examples).

The Noncentral F Distribution

Once Fc, df1, df2, and λ are determined, power calculation is completed by use of the noncentral F distribution. Tables of this distribution are provided by Rotton and Schonemann (1978), Tiku (1967), and most textbooks on ANOVA. Table powers are usually indexed by df1, df2, and phi (ϕ)-rather than λ . According to Winer, Brown, and Michels (1991, p. 408), λ can be converted to ϕ using the following algorithm.

 $\phi = SQRT[\lambda / (number of effect levels)]$

Laubscher (1960) describes a square root normal approximation of the noncentral \underline{F} distribution (formula 6) which may be used to calculate the power of an \underline{F} ratio using a hand calculator and tables of the central \underline{F} and \underline{Z} distributions. While both Cohen (1988, p. 550) and Laubscher (1960) describe a cube root normal approximation, Laubscher concluded that the square root approximation was slightly more accurate for the tested data set. Cohen (1988, p. 550) comments that Laubscher's square root normal approximation of noncentral \underline{F} "gave excellent agreement with exact value determinations given in the literature...except when n and f are small," but does not define small. A somewhat simplified version of Cohen's adaptation of Laubscher's square root approximation of the probabilities given by the noncentral \underline{F} distribution is:

$$\frac{X1}{X2} = \frac{(df1 + 2 * \lambda)}{(df1 * Fc)} / \frac{(df1 + \lambda)}{(df2 + \lambda)}$$

$$\frac{Z}{Z} = \frac{SQRT[2 * (df1 + \lambda) - X1] - SQRT[(2 * df2 - 1) * X2]}{SQRT(X1 + X2)}$$

Power $>= 1 - [Probability of (<math>\underline{Z}$)]

Where:

df1 = numerator degrees of freedom of the original F ratio.

 $\underline{df2} = denominator degrees of freedom of the original <math>\underline{F}$ ratio.

 λ = the non-centrality parameter.

 \underline{Fc} = the value of the critical \underline{F} ratio given the original \underline{F} ratio degrees of freedom and significance criterion.

 $\underline{Z} = \underline{A} \ \underline{Z}$ value, the probability of which may be determined using a table of proportions of area under the standard normal curve. This probability is the probability of a Type II error (i.e., β).

The following computer programs and associated manuals were used in the preparation of this manuscript: Statistical design analysis system (Bavry, in press); Stat-Power statistical design analysis system (Bavry, 1991); and Statistical power analysis: A computer program (Borenstein & Cohen, 1988). A review of computer programs used to calculate power analyses may be found elsewhere (Goldstein, 1989).

Effect Size

Calculating Effect Size

Calculating the power of a completed \underline{F} test is thus a relatively straightforward task given the significance criterion, \underline{F} ratio degrees of freedom, and λ . As mentioned above, however, power analysis is primarily useful in predicting the number of observations needed to obtain a significant

effect, if one exists, with a given power, or the probability that a statistically significant effect would have been obtained if one had existed. In both cases, the F ratio necessary to predict λ does not exist and must be estimated. The discerning reader will realize that it may be difficult to estimate λ on an a priori basis. Several investigators have proposed ANOVA-based measures of effect size to assist in λ estimation, as reviewed by Tatsuoka (1993). Probably the most intuitive is Cohen's \underline{f} , which is defined as the standard deviation of the effect means divided by the (common) withincell standard deviation (Cohen, 1988, pp. 274-275). While Cohen (1988, pp. 215-406) provides several examples of the standard deviation of the effect means calculations, a detailed explanation of the (common) within-cell standard deviation is not found. Hedges (1981), however, demonstrated that the square root of the F ratio's within-cell mean square error term provides the best unbiased estimator of the within-cell standard deviation. Thus, the terminology of Cohen (1988) and Hedges (1981) are adapted as:

Effect size $(\underline{f}) = \underline{SDm} / \underline{SDe}$

Where:

 $\underline{\underline{f}}$ = Cohen's ANOVA-based effect size (Cohen uses the letter $\underline{\underline{f}}$ to indicate effect size - this should not be confused with the uppercase $\underline{\underline{F}}$ which is used to denote the $\underline{\underline{F}}$ ratio).

SDm = The standard deviation of the effect means.
SDe = The square root of the within-cell mean square
error term.

The effect size numerator (SDm) is calculated using one of three techniques depending on the type of factor (main effect vs. interaction) and the number of levels. Calculation procedures for the effect size denominator (SDe) for a betweensubjects ANOVA design differs from those for a within-subjects ANOVA design. These are detailed below and numerical examples are provided in Appendix D. Before proceeding with the examples, a short description of the notation used is necessary. The capital letter "M" is used to indicate the mean of a cell, lower case letters are used to indicate the factor, and arabic numbers are used to indicate the factor level. A period will be used to indicate that a particular factor has been averaged. Thus: "Ma.." indicates the means associated with factor A; "Mal.." indicates the mean of factor A, level 1; "M.b." indicates the means associated with factor B; "M..c" indicates the means associated with factor C; "Mabc" indicates the cell means associated with the A x B x C interaction; and "M..." indicates the grand mean of all values in the data set. For within-subject designs, the notation for specific observations follows the same pattern where: "Mal..sl" indicates the average of subject 1's scores over level 1 of factor A and "M..c4s3"

indicates the average of subject 3's scores over level 4 of factor C.

The following examples are for an A (2 levels) x B (3 levels) x C (4 levels) design with 5 observations per cell. The \underline{SDm} is calculated in the same manner for both the within- and between-subjects designs. The same \underline{SDe} term is used to calculate the effect size of each factor in a between-subject design - in the same manner as a common mean square error term is used when calculating the \underline{F} ratio for each test of a between subjects design. The \underline{SDe} term is used to calculate the effect size of each factor in a within-subjects design varies, as does the mean square error term used when calculating the \underline{F} ratios of a within-subjects design.

The \underline{SDe} term for the A (2 levels) x B (3 levels) x C (4 levels) example with 5 independent observations in each cell is:

Or, more simply, the square root of the average cell variance:

Where: VAR is the variance.

The general \underline{SDe} term for a within-subjects ANOVA is the square root of the within-cell mean square error term used in the \underline{F} ratio for which the power is being calculated. A general example is given below and examples of specific calculations for the various effects may be found in Appendix D:

$$\underline{SDe} = SQRT \begin{bmatrix} 2 & 5 \\ \Sigma & [(\Sigma & (Max..sy - Max...)^2] \\ x=1 & y=1 \\ \hline 8 & (i.e., the \underline{F} ratio denominator \underline{df}) \end{bmatrix}$$

(1) Effect size of a main effect with 2 levels is calculated using:

$$\underline{f} = \begin{bmatrix} 0.5 * (maximum Ma.. - minimum Ma..) \\ \underline{SDe} \end{bmatrix}$$

Note: The standard deviation of two values is 0.5 * the difference between the two values.

(2) Effect size of a main effect with more than 2 levels is calculated using:

$$SQRT\{ \begin{bmatrix} \underline{N} \\ \Sigma \end{bmatrix} (M..cx - M...)^2] / \underline{N} \}$$

$$\underline{f} = \frac{1}{SDe}$$

(3) Interaction effect sizes are the square root of the summed squares of the contribution of each cell to the effect divided by the number of cells. The contribution of each cell's effect is calculated by removing the contributions of other factors to that cells effect (i.e., using the linear model). The process is similar to that used to calculate the sum of squares for an \underline{F} ratio interaction. For example, the effect size for Cohen's (1988) example 8.6 (pp. 368-372) A(2 levels) x B(3 levels) interaction would be calculated as:

Note: Calculating the cell contributions can become quite complex. A good guide for the factors and signs may be found in Kirk (1968). The X???s used to calculate the <u>SDm</u> for Cohen's example 8.6 A x B x C effect would be:

Xabc = Mabc - Mab. - Ma.c - M.bc + Ma.. + M.b. + M..c - M...

Converting Cohen's Effect Size to λ

Cohen's (1988) ANOVA-based measure of effect size can be converted to λ using the following algorithm.

 $\lambda = f^2$ * (the total number of observations analyzed for the effect)

The total number of observations analyzed for an effect is the number of observations used in calculating the error term and will differ for within- and between-subjects ANOVA designs. For example, the number of observations for the effects of an A (2 levels) x B (3 levels) x C (4 levels) ANOVA with 5 observations per cell, analyzed as a within- or between-subjects design would be:

Effect	Total Number of Observations Within-subjects	Total Number of Observations Between-subjects
A	10	120
В	15	120
AxB	15	. 120
C	20	120
AxC	20	120
BxC	120	120
AxBxC	120	120

A Note Concerning Cohen's Description of ANOVA Power Calculation
The power tables for ANOVA designs provided by Cohen (1988, pp. 273-406) require specification of: a desired significance criterion; an effect size; the <u>F</u> ratio numerator degrees of freedom; and the sample size. Cohen (1988, p. 365) indicates that it is necessary to use an adjusted samples size to cope with the discrepancy in denominator (error) degrees of freedom between one-way and higher-way ANOVA designs. Cohen (1988, p. 365) describes the calculation of sample size (<u>n</u>') as follows:

sample size =
$$\underline{n'}$$
 = $\frac{\text{denominator } \underline{df}}{\underline{u} + 1}$ + 1

Where:

 $\underline{\mathbf{u}}$ = the degrees of freedom associated with the numerator of the $\underline{\mathbf{F}}$ ratio for which power is to be calculated.

denominator \underline{df} = total number of observations in the analysis minus the total number of cells in the analysis.

An example calculation of n for each of the effects in a $2(A) \times 3(B) \times 4(C)$ ANOVA with 5 observations per cell (Cohen's example 8.6, p. 368-372) would be:

Total observations = 120 (i.e., 2 * 3 * 4 * 5) Total number of cells = 24 (i.e., 2 * 3 * 4) Denominator \underline{df} = 120 - 24 = 96

	Numerator	
Effect	<u>df</u>	<u>n</u>
A	1	49.0
В	2	33.0
C	3	25.0
$A \times B$	2	33.0
AxC	3	25.0
ВхС	6	14.7
AxBxC	6	14.7

This adjustment works well for a one-way ANOVA design. However, as noted by Koele (1982), and illustrated in Appendices B and C, using Cohen's technique to calculate the power of effects in higher-way ANOVA designs will result in an underestimation of the power of between-subjects design effects and overestimation of the power of within-subjects effects. It is thus suggested that Cohen's ANOVA-based effect size measure be converted to and/or from λ and noncentral \underline{F} distribution probabilities be used to estimate power. This will ensure accurate results and is, in addition, less complicated computationally.

Constant Correlation

An assumption in repeated measures ANOVA is that there is a "constant" correlation between pairs of observations on the same subject under different conditions (Winer, 1971, p. 516). (1971, p. 516) and others (Lipsey, 1990, pp. 79-84; Davidson, 1972, p. 448; Kraemer & Thiemann, 1987, pp. 45-52) suggest that SDe should be increased or decreased according to the constant correlation when attempting to estimate the SDe for a withinsubjects ANOVA design using existing data from a study with a between-subjects ANOVA design (details below). A problem occurs when deciding how to estimate the constant correlation. When comparing only two observations, the product-moment correlation may be used as an estimate of the constant correlation. Dr. Bavry (personal communication) and others (Silver & Dunlap, 1987; Silver & Hollingsworth, 1989; Viana, 1980, 1993) suggest that the best estimate of the constant correlation is calculated by averaging the Fisher's Z transform (Fisher, 1921) of all of the within-subjects between-cell correlations, then converting that Fisher's Z transform average back to a correlation coefficient. An numerical example of constant correlation calculation for data presented in Appendix A is given in Appendix E. Fisher's Z transform and its inverse are as follows (Silver & Dunlap, 1987).

Fisher's \underline{Z} transform is: $\underline{Z} = 0.5 * \log_e [(1+\underline{r})/(1-\underline{r})]$

The inverse transform is: $\underline{r} = (\underline{X} - 1) / (\underline{X} + 1)$

Where:

 \underline{r} = the correlation coefficient \underline{X} = exp_e (2 * \underline{Z})

Note: The constant correlation correction is only necessary when attempting to estimate the \underline{SDe} for a within-subjects ANOVA design using existing data from a study with a between-subjects ANOVA design.

According to Winer (1971, p. 516), the following correction should be used to adjust estimates of <u>SDe</u> obtained from between-subjects designs when calculating power analyses of <u>F</u> ratios involving repeated measures. The <u>SDe</u> of repeated measure interaction and main effects should be adjusted by multiplying <u>SDe</u> by (1-r), where r is the constant correlation for that effect. The <u>SDe</u> of between groups effects which are composed of repeated measures on each member of a group should be adjusted by multiplying <u>SDe</u> by (1 + W * r), where <u>W</u> is the tested effect degrees of freedom and r is the constant correlation for that effect.

Description of the Appendices

Appendix A contains the results of between-subjects and within-subjects ANOVA of data presented by Winer (1962, p. 324; 1971, p. 546). Appendices B and C contain the results of a power analysis of the data in Appendix A using the suggested noncentral \underline{F} distribution and Cohen's tables, respectively. A comparison of the results obtained using the two methods illustrates the tendency of Cohen's technique to overestimate between-subjects and underestimate within-subjects higher-way ANOVA effect powers. Appendix D contains a numerical example of the calculations necessary to obtain the data presented in Appendices B and C. Appendix E contains a numerical example of the use of Fisher's \underline{Z} transform to calculate the average correlation of data in Appendix A. Appendix F contains algorithms for converting values among ϕ , λ , and Cohen's effect size for ANOVA (\underline{f}) .

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Appendix A

Example Data and Analyses of Variance

The Raw Data (Winer, 1962, p. 324, 1971, p. 546):

	1	Period		P1			P2			P3	
Subject	Noise	Dial	D1.	D2	D3	D1	D2	D3		D2	D3
		Diai				_					
1	N1		45	53	60	40	52	57	28	37	46
2	N1		35	41	50	30	37	47	25	32	41
3	Nl		60	65	75	58	54	70	40	47	50
4	N2		50	48	61	25	34	51	16	23	35
5	N2		42	45	55	30	37	43	22	27	37
6	N2		56	60	77	40	39	57	31	29	46

Results of the analysis of Winer's data (1962, p. 324; 1971, p. 546) as a 2 (NOISE-between) x 3 (PERIOD-within) x 3 (DIAL-within) ANOVA

BETWEEN SUBJECTS							
SOURCE	SS	$\overline{\mathrm{DF}}$	MS	<u>F</u>	<u>P</u>		
NOISE	468.167	1	468.167	0.752	0.435		
ERROR	2491.111	4	622.778				
WITHIN SUBJECTS							
SOURCE	<u>ss</u>	$\overline{\mathrm{DF}}$	<u>MS</u>	F	<u>P</u>	G-G	H-F
PERIOD	3722.333	2	1861.167	63.389	0.000	0.000	0.00
NOISE*PERIOD	333.000	2	166.500	5.671	0.029	0.057	0.02
ERROR	234.889	. 8	29.361				
GREENHOUSE-GEISSE	R EPSILON:		0.6476 HU	JYNH-FELDT	EPSILON:	1.	.0000
DIAL	2370.333	2	1185.167	89.823	0.000	0.000	0.00
DIAL NOISE*DIAL	2370.333 50.333	2	1185.167 25.167	89.823 1.907	0.000 0.210	0.000 0.215	0.00
NOISE*DIAL	50.333 105.556	2	25.167 13.194		0.210	0.215	
NOISE*DIAL ERROR	50.333 105.556	2	25.167 13.194	1.907	0.210	0.215	0.21
NOISE*DIAL ERROR GREENHOUSE-GEISSE	50.333 105.556 R EPSILON: 10.667	2	25.167 13.194 0.9171 HU	1.907 JYNH-FELDT	0.210 EPSILON:	0.215	0.21
NOISE*DIAL ERROR GREENHOUSE-GEISSE PERIOD*DIAL	50.333 105.556 R EPSILON: 10.667	2 8 4	25.167 13.194 0.9171 HT 2.667	1.907 JYNH-FELDT 0.336	0.210 EPSILON: 0.850	0.215 1. 0.729	0.21

Results of the analysis of Winer's data (1962, p. 324; 1971, p. 546) as a 2 (NOISE-between) x 3 (PERIOD-between) x 3 (DIAL-between) ANOVA

SOURCE	SS	$\overline{\text{DF}}$	MS	$\underline{\mathbf{F}}$	<u>P</u>
NOISE	468.167	1	468.167	5.696	0.022
PERIOD	3722.333	2	1861.167	22.646	0.000
DIAL	2370.333	2	1185.167	14.421	0.000
NOISE*PERIOD	333.000	2	166.500	2.026	0.147
NOISE*DIAL	50.333	2	25.167	0.306	0.738
PERIOD*DIAL	10.667	4	2.667	0.032	0.998
NOISE*PERIOD*DIAL	11.333	4	2.833	0.034	0.998
ERROR	2958.667	36	82.185		

Appendix B

Power Calculations using the noncentral F distribution

POWER of Winer's (1962, p. 324; 1971, p. 546) 2(NOISE-between) x 3(PERIOD-within) x 3(DIAL-within) ANOVA example using Bavry's Non-central Cumulative \underline{F} Probability calculation.

Factor	<u>d</u>	<u>f</u>	- λ	Non-central Cumulative	Power $(1 - \beta)$	
140001	Numerator	Denominator		Probability (β)	(1 - μ)	
NOISE	1	4	0.752	0.896	0.104 +	
PERIOD	2	8	126.778	0.000	0.999	
NOISE*PERIOD	2	8	11.342	0.303	0.697	
DIAL	2	8	179.652	0.000	0.999	
NOISE*DIAL	2	8	3.815	0.714	0.286 +	
PERIOD*DIAL	4	16	1.343	0.893	0.107 +	
NOISE*PERIOD*DIAL	4	16	1.427	0.889	0.111 +	

POWER of Winer's (1962, p. 324; 1971, p. 546) 2(NOISE-between) x 3(PERIOD-between) x 3(DIAL-between) ANOVA data using Bavry's Non-central Cumulative \underline{F} Probability calculation.

Factor	₫	<u>lf</u>	λ	Non-central Cumulative	Power $(1 - \beta)$	
FACCOL	Numerator Denomi		X	Probability (β)	(1 - β)	
NOISE	1	36	5.697	0.358	0.642	
PERIOD	2	36	45.292	0.000	1.000	
DIAL	2	36	28.841	0.002	0.998	
NOISE*PERIOD	2	36	4.052	0.610	0.390 +	
NOISE*DIAL	2	36	0.612	0.905	0.095 +	
PERIOD*DIAL	4	36	0.130	0.944	0.056 +	
NOISE*PERIOD*DIAL	4	36	0.138	0.944	0.056 +	

⁺ These power values are given to illustrate the use of the cited formulae. They are not indicative of the power of the original \underline{F} ratio because the original \underline{F} ratio did not reach significance at the 0.05 level.

Appendix C

Power Calculations using Cohen's tables and technique

POWER of Winer's (1962, p. 324; 1971, p. 546) 2(NOISE-between) x 3(PERIOD-within) x 3(DIAL-within) ANOVA example using Cohen's method.

	<u>u</u>	<u>n</u> /group	<u>n</u> '	SDm	<u>SDe</u>	<u>f</u>	POWER
NOISE	1.000	3.000	3.000	2.944	8.318	0.354	0.111 +
PERIOD	2.000	6.000	6.000	8.302	3.129	2.653	0.999
NOISE*PERIOD	2.000	6.000	6.000	2.483	3.129	0.794	0.705 +
DIAL	2.000	6.000	6.000	6.625	2.097	3.159	0.999
NOISE*DIAL	2.000	6.000	6.000	0.965	2.097	0.460	0.337 +
PERIOD*DIAL	4.000	9.800	10.800	0.444	2.818	0.157	0.117 +
NOISE*PERIOD*DIAL	4.000	9.800	10.800	0.458	2.818	0.163	0.123 +

POWER of Winer's (1962, p. 324; 1971, p. 546) 2(NOISE-between) x 3(PERIOD-between) x 3(DIAL-between) ANOVA data using Cohen's method.

	u	n/group	n'	SDm	SDe	£	POWER
NOISE	1.000	27.000	19.000	2.944	9.065	0.324	0.573
PERIOD	2.000	18.000	13.000	8.302	9.065	0.916	0.999
DIAL	2.000	18.000	13.000	6.625	9.065	0.731	0.980
NOISE*PERIOD	2.000	9.000	13.000	2.483	9.065	0.274	0.293 +
NOISE*DIAL	2.000	9.000	13.000	0.965	9.065	0.106	0.078 +
PERIOD*DIAL	4.000	6.000	8.200	0.444	9.065	0.049	0.051 +
NOISE*PERIOD*DIAL	4.000	3.000	8.200	0.458	9.065	0.051	0.053 +

⁺ These power values are given to illustrate the use of the cited formulae. They are not indicative of the power of the original \underline{F} ratio because the original \underline{F} ratio did not reach significance at the 0.05 level.

Appendix D

Numerical Examples of Power Calculation

Calculation of SDe for the data from Winer's (1962, p. 324; 1971, p. 546) 2 x 3 x 3 example analyzed as a 2(NOISE-between) x 3(PERIOD-between) x 3(DIAL-between) design.

N#P#D#S 1 1 1 . Mn= 46.6667 Var= 158.3333 1 1 2 . Mn= 53.0000 Var= 144.0000 1 1 3 . Mn= 61.6667 Var= 158.3333 1 2 1 . Mn= 42.6667 Var= 201.3333 1 2 2 . Mn= 47.6667 Var= 86.3333 1 2 3 . Mn= 58.0000 Var= 133.0000 1 3 1 . Mn= 31.0000 Var= 63.0000 1 3 2 . Mn= 38.6667 Var= 58.3333 1 3 3 . Mn= 45.6667 Var= 20.3333 2 1 1 . Mn= 49.3333 Var= 49.3333 2 1 2 . Mn= 51.0000 Var= 63.0000 2 1 3 . Mn= 129.3333 64.3333 Var= 2 2 1 . Mn= 31.6667 58.3333 Var= 2 2 2 . Mn= 36.6667 Var= 6.3333 2 2 3 . Mn= 50.3333 Var= 49.3333 2 3 1 . Mn= 23.0000 Var= 57.0000 2 3 2 . Mn= 26.3333 Var= 9.3333 2 3 3 . Mn= 39.3333 Var= 34.3333 Grand Average = 44.2777 Var= 82.1852

 $\underline{SDe} = SQRT(82.1852) = 9.0656$

Power Calculation for NOISE Effect:

Calculation of SDm for the NOISE effect:

```
N#P#D#S#
            Xi =Mn...-M....
          2.944 = 47.222 44.278
 2 . . . -2.944 =41.333 44.278
                                                    Sum of Squares
                                 Xi^2
                                             (Xi^2) * (Observations/average)
      Χi
    2.944
                                8.670
                                                         234.083
    -2.944
                                8.670
                                                         234.083
                        SUM = 17.340
                                                   SUM = 468.167
SDm = Sqrt(\Sigma(Xi^2) / I) = SQRT(17.340 / 2) = 2.944
           i=1
```

Calculation of SDe for the NOISE effect:

```
N#P#D#S#
                Yj =Mn..s -Mn...
 1 . . 1
             -0.778 46.444 47.222
 1 . . 2
             -9.667 37.556 47.222
 1 . . 3
            10.444 57.667 47.222
 2 . . 4
             -3.222 38.111 41.333
 2 . . 5
             -3.778 37.556 41.333
 2 . . 6
              7.000 48.333 41.333
                                                     Sum of Squares
                                 Yj^2
                                              (Yj^2) * (Observations/average)
      Υi
     -0.778
                                0.605
                                                            5.444
     -9.667
                                93.444
                                                          841.000
     10.444
                              109.086
                                                          981.778
     -3.222
                                10.383
                                                           93.444
     -3.778
                                14.272
                                                          128.444
     7.000
                                49.000
                                                          441.000
                                                    SUM =2491.111
                         SUM = 276.790
SDe = Sqrt(\Sigma (Yj<sup>2</sup>) / denominator df) = SQRT(276.790 / 4) = 8.318
            j=1
```

Note: Cohen's Denominator df = (6/2 - 1) * 2 = 4

Power Calculation for the PERIOD and NOISE*PERIOD Effects:

Calculation of SDm for the PERIOD effect:

```
N#P#D#S#
                Xi =M.p.. -M....
 . 1 . .
             10.055 54.333 44.278
 . 2 . .
              0.222 44.500 44.278
 . 3 . .
             -10.278 34.000 44.278
                                                    Sum of Squares
                                            (Xi^2) * (Observations/average)
      Χi
                                 Xi^2
   10.055
                                                        1819.854
                              101.103
    0.222
                                0.049
                                                            .882
                                                        1901.466
   -10.278
                              105.637
                         SUM = 206.789
                                                  SUM = 3722.202
SDm = Sqrt(\Sigma(Xi^2) / I) = SQRT(206.789 / 3) = 8.302
            i=1
```

Calculation of SDm for the NOISE*PERIOD effect:

```
N#P#D#S# Xi =Mnp.. -M.p.. -Mn... +M....

1 1 . . . -3.4995 53.778 54.333 47.222 44.277

1 2 . . . 2.0001 49.444 44.500 47.222 44.277

1 3 . . 1.5001 38.444 34.000 47.222 44.277

2 1 . . 3.5006 54.889 54.333 41.333 44.277

2 2 . . -1.9997 39.556 44.500 41.333 44.277

2 3 . . -1.4997 29.556 34.000 41.333 44.277
```

Sum of Squares Xi^2 (Xi^2) * (Observations/average) Χi -3.499 12.246 110.219 2.000 4.000 36.004 1.500 2.250 20.253 110.288 3.500 12.254 -1.999 3.999 35.989 -1.499 2.249 20.242 SUM = 36.999SUM = 332.9937

 $\frac{\text{SDm}}{\text{SDm}} = \text{Sqrt}(\Sigma (Xi^2) / I) = \text{SQRT}(36.999 / 6) = 2.483$ i=1

Calculation of SDe for the PERIOD and NOISE*PERIOD Effects:

```
N#P#D#S#
             Yj =Mnp.s -Mnp.. -Mn..s +Mn...
11.1
          -0.333 52.667 53.778 46.445 47.222
11.2
          -2.111 42.000 53.778 37.556 47.222
11.3
           2.444 66.667 53.778 57.667 47.222
2 1 . 4 - 1.333 53.000 54.889 38.111 41.333
21.5
          -3.778 47.333 54.889 37.556 41.333
21.6
           2.445 64.333 54.889 48.333 41.333
12.1
           1.000 49.667 49.445 46.445 47.222
12.2
          -1.778 38.000 49.445 37.556 47.222
12.3
           0.778 60.667 49.445 57.667 47.222
22.4
           0.333 36.667 39.556 38.111 41.333
2 2 . 5
           0.889 36.667 39.556 37.556 41.333
22.6
          -1.222 45.333 39.556 48.333 41.333
13.1
          -0.667 37.000 38.445 46.445 47.222
1 3 . 2
           3.889 32.667 38.445 37.556 47.222
1 3 . 3
          -3.222 45.667 38.445 57.667 47.222
23.4
          -1.667 24.667 29.556 38.111 41.333
2 3 . 5
          2.889 28.667 29.556 37.556 41.333
2 3 . 6
          -1.222 35.333 29.556 48.333 41.333
```

		Sum of Square	s
Υj	Yj^2	(Yj^2) * (Observation	ns/average)
-0.333	0.111	0.333	
-2.111	4.457	13.372	
2.444	5.975	17.926	
1.333	1.778	5.333	
-3.778	14.273	42.820	
2.445	5.976	17.929	
1.000	1.000	3.001	
-1.778	3.161	9.483	
0.778	0.605	1.815	
0.333	0.111	0.333	
0.889	0.790	2.371	
-1.222	1.494	4.482	
-0.667	0.445	1.334	
3.889	15.125	45.375	
-3.222	10.383	31.148	
-1.667	2.778	8.333	
2.889	8.346	25.039	
-1.222	1.494	4.482	
	SUM = 78.303	SUM = 234.910	

 $\underline{SDe} = Sqrt(\Sigma (Yj^2) / denominator \underline{df}) = SQRT(78.303 / 8) = 3.129$ j=1

Power Calculation for the PERIOD Effect:

Power Calculation for the NOISE*PERIOD Effect:

Note: Denominator df = (18/3 - 1) * 3 = 15

Power Calculation for the DIAL and NOISE*DIAL Effects:

Calculation of SDm for the DIAL effect:

N#P#D#S#	Xi =MdM
1 .	-6.889 37.389 44.278
2 .	-2.056 42.222 44.278
3 .	8.944 53.222 44.278

		Sum of Squares
Xi	Xi^2	(Xi^2) * (Observations/average)
-6.889	47.458	854.250
-2.056	4.227	76.088
8.944	79.995	1439.912
	SUM = 131.681	SUM = 2370.251

 $\frac{3}{\text{SDm}} = \text{Sqrt}(\Sigma (Xi^2) / I) = \text{SQRT}(131.681 / 3) = 6.625$ i=1

Calculation of \underline{SDm} for the NOISE*DIAL effect:

N‡	P	#D#	‡S#	Xi :	=Mn.d.	-Md.	-Mn	+M
1		1		-0.221	40.111	37.389	47.222	44.278
1		2		1.278	46.444	42.222	47.222	44.278
1		3		-1.055	55.111	53.222	47.222	44.278
2		1		0.222	34.667	37.389	41.333	44.278
2		2		-1.277	38.000	42.222	41.333	44.278
2		3		1.056	51.333	53.222	41.333	44.278

		Sum OI Squares
Xi	Xi^2	(Xi^2) * (Observations/average)
-0.221	0.049	0.439
1.278	1.634	14.702
-1.055	1.113	10.021
0.222	0.050	0.446
-1.277	1.632	14.684
1.056	1.115	10.036
	SUM = 5.592	SUM = 50.326

$$\frac{\text{SDm}}{\text{SDm}} = \text{Sqrt}(\Sigma (Xi^2) / I) = \text{SQRT}(5.592 / 6) = 0.965$$

$$i=1$$

Calculation of SDe for the DIAL and NOISE*DIAL Effects:

```
N#P#D#S#
               Yj =Mn.ds -Mn.d. -Mn..s +Mn...
1 . 1 1
             -1.667 37.667 40.111 46.444 47.222
1 . 1 2
             -0.444 30.000 40.111 37.556 47.222
1 . 1 3
             2.111 52.667 40.111 57.667 47.222
2 . 1 4
             -1.111 30.333 34.667 38.111 41.333
2 . 1 5
             0.444 31.333 34.667 37.556 41.333
2.16
             0.667 42.333 34.667 48.333 41.333
1 . 2 1
             1.667 47.333 46.444 46.444 47.222
             -0.111 36.667 46.444 37.556 47.222
1 . 2 2
1 . 2 3
            -1.556 55.333 46.444 57.667 47.222
2 . 2 4
             0.222 35.000 38.000 38.111 41.333
2 . 2 5
             2.111 36.333 38.000 37.556 41.333
2 . 2 6
             -2.333 42.667 38.000 48.333 41.333
1 . 3 1
             0.000 54.333 55.111 46.444 47.222
1 . 3 2
           0.556 46.000 55.111 37.556 47.222
1 . 3 3
             -0.556 65.000 55.111 57.667 47.222
2 . 3 4
             0.889 49.000 51.333 38.111 41.333
2 . 3 5
             -2.556 45.000 51.333 37.556 41.333
2 . 3 6
             1.667 60.000 51.333 48.333 41.333
```

Sum of Squares (Yi^2) * (Observations/average) Υj Yj^2 -1.667 2.778 8.333 -0.444 0.198 0.593 2.111 4.457 13.370 -1.1111.235 3.704 0.444 0.198 0.593 0.667 0.444 1.333 1.667 2.778 8.333 -0.111 0.012 0.037 -1.556 2.420 7.259 0.222 0.049 0.148 2.111 4.457 13.370 -2.333 5.444 16.333 0.000 0.000 0.000 0.556 0.309 0.926 -0.556 0.309 0.926 0.889 0.790 2.370 -2.556 6.531 19.593 1.667 2.778 8.333 SUM = 35.185SUM = 105.556

 $\frac{SDe}{SDe} = Sqrt(\Sigma (Yj^2) / denominator \underline{df}) = SQRT(35.185 / 8) = 2.097$ j=1

Power Calculation for the DIAL Effect:

COHEN BAVRY Effect Size = $\underline{f} = \underline{SDm} / \underline{SDe}$ $\lambda = SSm / MSe$ Effect Size = $\underline{f} = 6.625 / 2.097$ $\lambda = 2370.333 / (105.556/8)$ Effect Size = 3.159 $\lambda = 179.652$ $\underline{u} = 2.0$ $\underline{DFm} = 2.0$ $\underline{DFm} = 2.0$ $\underline{DFe} = 8.0$ Effect power = 1.000 (0.9999) Effect power = 1.000 (0.9999)

Power Calculation for the NOISE*DIAL Effect:

Note : Denominator df = (18/3 - 1) * 3 = 15

Power Calculation for the PERIOD*DIAL and NOISE*PERIOD*DIAL Effects:

Calculation of SDm for the PERIOD*DIAL effect:

```
N#P#D#S#
             Xi = M.pd..-M..d..-M.p...+M....
. 1 1 .
            0.556 48.000 37.389 54.333 44.278
. 1 2 .
           -0.277 52.000 42.222 54.333 44.278
           -0.277 63.000 53.222 54.333 44.278
. 1 3 .
. 21.
           -0.444 37.167 37.389 44.500 44.278
. 2 2 .
           -0.277 42.167 42.222 44.500 44.278
. 2 3 .
           0.723 54.167 53.222 44.500 44.278
 31.
           -0.111 27.000 37.389 34.000 44.278
. 3 2 .
           0.556 32.500 42.222 34.000 44.278
           -0.444 42.500 53.222 34.000 44.278
                                                     Sum of Squares
      Χi
                                 Xi^2
                                              (Xi^2) * (Observations/average)
     0.556
                                 0.309
                                                        1.855
                                 0.077
                                                        0.460
    -0.277
    -0.277
                                 0.077
                                                        0.460
    -0.444
                                                        1.183
                                 0.197
    -0.277
                                 0.077
                                                        0.460
```

0.523

0.012

0.309

0.197

SUM = 1.778

3.136

0.074

1.855

1.183

SUM = 10.667

 $SDm = Sqrt(\Sigma(Xi^2) / I) = SQRT(1.778 / 9) = 0.444$ i=1

0.723

-0.111

0.556

-0.444

Calculation of SDm for the NOISE*PERIOD*DIAL effect:

```
N#P#D#S#
           Xi = Mnpd.-Mnp.. -Ma.d. -M.pd. +Mn... +M.p.. +M..d. -M....
1 1 1 . -0.555 46.667 53.778 40.111 48.000 47.222 54.333 37.389 44.277
         0.278 53.000 53.778 46.444 52.000 47.222 54.333 42.222 44.277
113.
         0.278 61.667 53.778 55.111 63.000 47.222 54.333 53.222 44.277
121.
          0.779 42.667 49.444 40.111 37.167 47.222 44.500 37.389 44.277
1 2 2 .
        -0.721 47.667 49.444 46.444 42.167 47.222 44.500 42.222 44.277
1 2 3 .
         -0.055 58.000 49.444 55.111 54.167 47.222 44.500 53.222 44.277
1 3 1 .
        -0.221 31.000 38.444 40.111 27.000 47.222 34.000 37.389 44.277
         0.446 38.667 38.444 46.444 32.500 47.222 34.000 42.222 44.277
1 3 3 .
        -0.221 45.667 38.444 55.111 42.500 47.222 34.000 53.222 44.277
2 1 1 .
         0.555 49.333 54.889 34.667 48.000 41.333 54.333 37.389 44.277
2 1 2 . -0.278 51.000 54.889 38.000 52.000 41.333 54.333 42.222 44.277
2 1 3 . -0.278 64.333 54.889 51.333 63.000 41.333 54.333 53.222 44.277
        -0.778 31.667 39.556 34.667 37.167 41.333 44.500 37.389 44.277
221.
222.
          0.722 36.667 39.556 38.000 42.167 41.333 44.500 42.222 44.277
          0.055 50.333 39.556 51.333 54.167 41.333 44.500 53.222 44.277
2 3 1 .
          0.222 23.000 29.556 34.667 27.000 41.333 34.000 37.389 44.277
        -0.445 26.333 29.556 38.000 32.500 41.333 34.000 42.222 44.277
         0.222 39.333 29.556 51.333 42.500 41.333 34.000 53.222 44.277
```

Sum of Squares

		4
Хj	Xj^2	(Xj^2) * (Observations/average)
-0.555	0.308	0.924
0.278	0.077	0.232
0.278	0.077	0.232
0.779	0.607	1.821
-0.721	0.520	1.560
-0.055	0.003	0.009
-0.221	0.049	0.147
0.446	0.199	0.597
-0.221	0.049	0.147
0.555	0.308	0.924
-0.278	0.077	0.232
-0.278	0.077	0.232
-0.778	0.605	1.816
0.722	0.521	1.564
0.055	0.003	0.009
0.222	0.049	0.148
-0.445	0.198	0.594
0.222	0.049	0.148
	SUM = 3.778	SUM = 11.333

 $\frac{18}{\underline{SDm}} = \frac{18}{\sqrt{\Sigma}} = \frac{18}{\sqrt{\Sigma}}$

Calculation of SDe for the PERIOD*DIAL and NOISE*PERIOD*DIAL Effects:

```
Yi^2
N#P#D#S#
                   Yi = Mnpds -Mnpd. -Mnp.s -Mn.ds +Mnp.. +Mn.d. +Mn..s -Mn...
1 1 1 1
          1.234
                  1.111 45.000 46.666 52.667 37.667 53.778 40.111 46.444 47.222
          0.310
                  0.557 35.000 46.666 42.000 30.000 53.778 40.111 37.556 47.222
1 1 1 2
1 1 1 3
          2.776
                 -1.666 60.000 46.666 66.667 52.667 53.778 40.111 57.667 47.222
2 1 1 4
         13.454
                  3.668 50.000 49.333 53.000 30.333 54.889 34.667 38.111 41.333
2 1 1 5
          0.048
                 -0.220 42.000 49.333 47.333 31.333 54.889 34.667 37.556 41.333
2 1 1 6
         11.854
                 -3.443 56.000 49.333 64.333 42.333 54.889 34.667 48.333 41.333
1 1 2 1
          0.309
                 -0.556 53.000 53.000 52.667 47.333 53.778 46.444 46.444 47.222
1 1 2 2
          0.012
                 -0.111 41.000 53.000 42.000 36.667 53.778 46.444 37.556 47.222
1 1 2 3
                  0.667 65.000 53.000 66.667 55.333 53.778 46.444 57.667 47.222
          0.445
2 1 2 4
          1.777
                 -1.333 48.000 51.000 53.000 35.000 54.889 38.000 38.111 41.333
2 1 2 5
          0.307
                 -0.554 45.000 51.000 47.333 36.333 54.889 38.000 37.556 41.333
2 1 2 6
          3.568
                  1.889 60.000 51.000 64.333 42.667 54.889 38.000 48.333 41.333
1 1 3 1
          0.309
                 -0.556 60.000 61.667 52.667 54.333 53.778 55.111 46.444 47.222
                 -0.444 50.000 61.667 42.000 46.000 53.778 55.111 37.556 47.222
1 1 3 2
          0.197
1 1 3 3
          1.000
                  1.000 75.000 61.667 66.667 65.000 53.778 55.111 57.667 47.222
2 1 3 4
          5.443
                 -2.333 61.000 64.333 53.000 49.000 54.889 51.333 38.111 41.333
2 1 3 5
                  0.779 55.000 64.333 47.333 45.000 54.889 51.333 37.556 41.333
          0.607
2 1 3 6
                  1.556 77.000 64.333 64.333 60.000 54.889 51.333 48.333 41.333
          2.421
1 2 1 1
                 -1.224 40.000 42.667 49.667 37.667 49.444 40.111 46.444 47.222
          1.498
1 2 1 2
          0.605
                 -0.778 30.000 42.667 38.000 30.000 49.444 40.111 37.556 47.222
                  1.999 58.000 42.667 60.667 52.667 49.444 40.111 57.667 47.222
1 2 1 3
          3.996
2 2 1 4
          7.113
                 -2.667 25.000 31.667 36.667 30.333 39.555 34.667 38.111 41.333
2 2 1 5
                  0.778 30.000 31.667 36.667 31.333 39.555 34.667 37.556 41.333
          0.605
2 2 1 6
          3.568
                  1.889 40.000 31.667 45.333 42.333 39.555 34.667 48.333 41.333
1 2 2 1
          5.968
                  2.443 52.000 47.667 49.667 47.333 49.444 46.444 46.444 47.222
1 2 2 2
          0.789
                  0.888 37.000 47.667 38.000 36.667 49.444 46.444 37.556 47.222
1 2 2 3
         11.116
                 -3.334 54.000 47.667 60.667 55.333 49.444 46.444 57.667 47.222
          0.000
2 2 2 4
                 -0.001 34.000 36.667 36.667 35.000 39.555 38.000 38.111 41.333
                  1.111 37.000 36.667 36.667 36.333 39.555 38.000 37.556 41.333
2 2 2 5
          1.234
2 2 2 6
                 -1.112 39.000 36.667 45.333 42.667 39.555 38.000 48.333 41.333
          1.237
1 2 3 1
                 -1.223 57.000 58.000 49.667 54.333 49.444 55.111 46.444 47.222
          1.496
                 -0.111 47.000 58.000 38.000 46.000 49.444 55.111 37.556 47.222
1 2 3 2
          0.012
1 2 3 3
                  1.333 70.000 58.000 60.667 65.000 49.444 55.111 57.667 47.222
          1.777
2 2 3 4
          7.108
                  2.666 51.000 50.333 36.667 49.000 39.555 51.333 38.111 41.333
2 2 3 5
                -1.889 43.000 50.333 36.667 45.000 39.555 51.333 37.556 41.333
          3.568
2 2 3 6
          0.605
                 -0.778 57.000 50.333 45.333 60.000 39.555 51.333 48.333 41.333
1 3 1 1
                  0.110 28.000 31.000 37.000 37.667 38.444 40.111 46.444 47.222
          0.012
                  0.222 25.000 31.000 32.667 30.000 38.444 40.111 37.556 47.222
1 3 1 2
          0.049
                 -0.334 40.000 31.000 45.667 52.667 38.444 40.111 57.667 47.222
1 3 1 3
          0.112
2 3 1 4
          1.000
                 -1.000 16.000 23.000 24.667 30.333 29.555 34.667 38.111 41.333
2 3 1 5
          0.308
                -0.555 22.000 23.000 28.667 31.333 29.555 34.667 37.556 41.333
                  1.556 31.000 23.000 35.333 42.333 29.555 34.667 48.333 41.333
2 3 1 6
          2.421
                 -1.890 37.000 38.667 37.000 47.333 38.444 46.444 46.444 47.222
1 3 2 1
          3.572
                 -0.779 32.000 38.667 32.667 36.667 38.444 46.444 37.556 47.222
1 3 2 2
          0.607
                  2.666 47.000 38.667 45.667 55.333 38.444 46.444 57.667 47.222
1 3 2 3
          7.108
2 3 2 4
          1.777
                  1.333 23.000 26.333 24.667 35.000 29.555 38.000 38.111 41.333
2 3 2 5
                -0.555 27.000 26.333 28.667 36.333 29.555 38.000 37.556 41.333
          0.308
2 3 2 6
                 -0.778 29.000 26.333 35.333 42.667 29.555 38.000 48.333 41.333
          0.605
                  1.777 46.000 45.667 37.000 54.333 38.444 55.111 46.444 47.222
1 3 3 1
          3.158
```

Calculation of <u>SDe</u> for the PERIOD*DIAL and NOISE*PERIOD*DIAL Effects (continued):

```
N#P#D#S# Yj^2 Yi = Mnpds -Mnpd. -Mnp.s -Mn.ds +Mnp.. +Mn.d. +Mn..s -Mn...

1 3 3 2 0.308 0.555 41.000 45.667 32.667 46.000 38.444 55.111 37.556 47.222

1 3 3 3 5.448 -2.334 50.000 45.667 45.667 65.000 38.444 55.111 57.667 47.222

2 3 3 4 0.112 -0.334 35.000 39.333 24.667 49.000 29.555 51.333 38.111 41.333

2 3 3 6 0.605 -0.778 46.000 39.333 35.333 60.000 29.555 51.333 48.333 41.333

127.111 -0.006
```

 $\underline{SDe} = Sqrt(\Sigma (Yj^2) / denominator \underline{df}) = SQRT(127.111 / 16) = 2.818$ j=1

Power Calculation for the PERIOD*DIAL effect:

Power Calculation for the NOISE*PERIOD*DIAL Effect:

Note: Denominator df = (54/5 - 1) * 5 = 49

Appendix E

Calculation of the Average Correlation of Data from Appendix A

		P1			P2			Р3		
		D1	D2	D3	D1	D2	D3	D1	D2	D3
										
P1 :	D1		.9315	.9567	.6881	.4275	.8151	.5789	.3888	.5396
P1 :	D2			.9514	.8737	.6726	.9195	.8066	.6321	.8021
P1 :	D3				.7116	.4163	.7959	.6693	.3922	.6568
P2 :	D1					.8655	.9157	.9665	.9183	.9212
P2 :	D2						.8019	.7890	.9188	.8402
P2 :	D3							.8332	.8072	.8464
P3 :	D1								.8928	.9554
P3 :	D2									.8642
P3 :	D3									

Fisher's Z Transform of Correlation Matrices*:

Correlation Matrices:

			Pl			P2			Р3		
		D1	D2	D3	D1	D2	D3	D1	D2	D3	
P1	D1		1.669	1.905	0.844	0.457	1.142	0.661	0.410	0.604	
P1	D2			1.847	1.348	0.815	1.586	1.117	0.745	1.104	
P1	D3				0.890	0.443	1.087	0.810	0.414	0.787	
P2	D1					1.315	1.561	2.036	1.578	1.597	
P2	D2		9 1				1.104	1.069	1.581	1.222	
P2	D3							1.198	1.119	1.243	
P3	D1								1.435	1.890	
P3	D2									1.310	
P3	D3										

^{*} Values were rounded to three significant digits.

Average Fisher's \underline{Z} = 1.1652 $x = \exp_e (2 * 1.1652) = 10.28$ Average Correlation = (10.28 - 1) / (10.28 + 1) = .8226

Appendix F

Useful Conversion Algorithms

- $\phi = SQRT(\lambda / (number of effect levels))$ (Winer et al., 1991, p. 408)
- ϕ = effect size * SQRT(the total number of observations on which the effect estimate is based) (Winer et al., 1991, p. 409)
- λ = effect size^2 * (the total number of observations on which the effect estimate is based) (adapted from Cohen, 1988, p. 550)
- $\lambda = \underline{F} * \underline{df1}$ Where: $\underline{df1}$ = the numerator degrees of freedom (J. L. Bavry, personal communication, September 14, 1995)
- λ = (Sum of Squares Between) / (Mean Square Error) (J. L. Bavry, personal communication, September 14, 1995)